

## Water Level Trend in the Barind Area

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### ABSTRACT

The water level trend, using monthly data of 50 observation wells – 2 in each of the 25 upazillas under Barind Multipurpose Development Authority command area in the district of Rajshahi, Bangladesh – was analyzed for the period of 1986-2004. To determine the lean season maximum and wet season minimum trends, depth to water level was regressed over the time span a 5-year moving average instead of raw data was employed in formulating the regression equation. The slope or inclination of the regression equation, which indicated the trend of depth to water level, was mapped. A composite trend map, combining both the maximum and minimum depths, was presented that delineated distinct zones with regards to their potentiality in the Barind area. About 2/3 of the area showed gradual fall in the water level both in dry and wet seasons. Most of the remaining area, situated in the west, east and south east, experienced lowering of the water level either in the post monsoon season or during the lean period. Only small areas in Shibganj and Gomastapur in the west and Naogaon in the east exhibited a rise in water level.

Keywords: Water level, Trend, Smoothing, Nonparametric regression, Moving average regression, Contour map, Composite trend map.

### 1. INTRODUCTION

The Barind Tract, located in the northwest Bangladesh, is a hard red-soil area characterized by an elevated landscape with a relatively harsh climate. Because of its topographic setting, the surface water resource of this area is also limited. Compared to the rest of the country, it has higher temperature and evaporation. The annual precipitation of this dry land is the lowest in Bangladesh. The Tract, however, is endowed with one of the most fertile soils of the country – suitable for growing all types of crop. In addition, owing to the elevated topography it is blessed by the nature as being comparatively free from inundation by the annual flood that the rest of the country experiences. It is also secured from ravages caused by cyclones every year elsewhere in Bangladesh. Moreover, the Brined Tract is

virtually safe from arsenic hazard that the country is currently facing. On the other hand, scarcity of surface water and lower rainfall compounded with higher temperature and evapotranspiration had rendered this land agriculturally backward. The entire tract had literally been a mono-cropped land with a cropping intensity of only 117%.

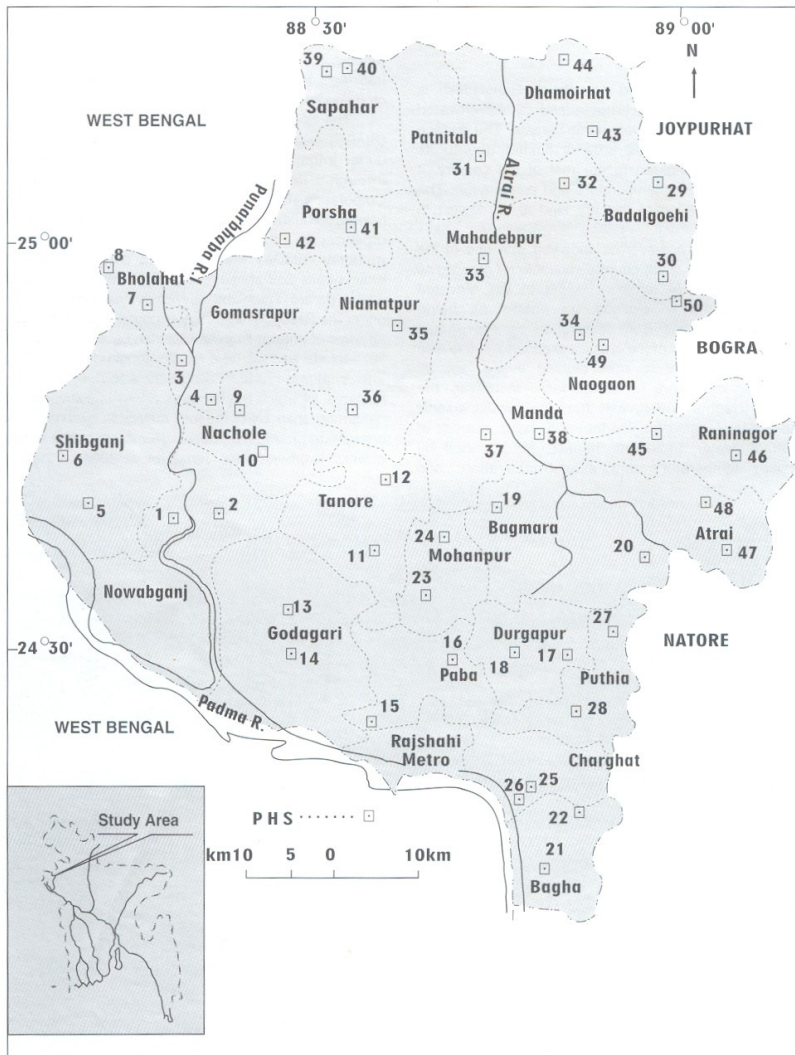


Figure 1: The Barind area

To bring the Tract under irrigation, the Barind Integrated Area Development Project (BIADP) was undertaken in 1985. The implementation of the project, through Bangladesh Agriculture Development Corporation (BADC), began in 1986 in 14 *upazillas* of greater Rajshahi District. In 1992 a separate organization – the Barind Multipurpose Development Authority (BMDA) was formed to carry on with the project in its 2<sup>nd</sup> phase. Presently much larger area of the Barind Tract and its vicinity has been incorporated in the BMDA. The area now comprises a total 25 *upazillas* of greater Rajshahi District between 24°23'-25°15' latitude and 88°02'- 88°57' longitude (Figure 1). The area under BMDA is about 0.77 million hectares of which 0.6 hectares (76%) cultivable. Till date more than 1/4 of the total cultivable land has been brought under irrigation coverage – the principal source of which is groundwater (see Jahan *et al.* (2004)).

So far, the BMDA has installed 6,682 Deep Tube Wells (DTWs) in its command area (BMDA, 2002). To extend the irrigation coverage even further, more DTWs are currently being sunk; and still more are in the pipeline. On the basis of overall recharge conditions, a study by the Master Plan Organization (MPO)/Groundwater Circle of Bangladesh Water Development Board (BWDB)/Sir M. McDonald and Partners found that the total number of (2 cusec) DTWs feasible for the areas was 8,827 [see BMDA (2001) cited in Jahan *et al.* (2004)]. It appears that the BMDA has been eyeing on this ad hoc estimate as their target. Meanwhile, however, concerns are being raised against the ever-increasing utilization of groundwater on the apprehension that we might already have reached the extraction limit of this valuable resource (e.g. Jahan (1997); BWDB (1992)).

Scarce surface waters have made groundwater the principal source for irrigation in the Barind. However, groundwater is also limited as there exist constraints for its development. Of these, the utmost is the groundwater availability in the area for safe extraction in terms of yearly groundwater recharge. Only annual renewable groundwater recharge represented by the present maximum (dry season) and minimum (wet season) depths to groundwater level is defined as the safe extraction. Potential in the storage occurring below the maximum depth to water level is not be considered as withdrawal from storage would, in fact, mean mining this natural endowment out like a non-renewable resource. The paper attempts to analyze the trend of groundwater level in the Barind area. The characteristics of both maximum and minimum depths to groundwater level will be looked into in detail.

## 2. GEOLOGICAL ASPECTS

In this section we briefly discuss two geological aspects, hydrology and climate of the Barind area.

### Hydrogeology

The study area is characterized by the north-south dome-shaped uplifted undulatory land in the central Barind Tract with a maximum elevation of 45 m above Mean Sea Level (MSL) (see Jahan and Ahmed (1997)). The central Barind Tract slopes both to the west and east with a gradient of 0.94 m/km (see BWDB (1989)). The western and northern parts of the area are undulatory, while the east and southeast are plane land. Floodplains of the rivers: Padma (Ganges), Mahananda, Atrai, Punarbhaba, etc. flowing through the Tract constitute about 46% of the total area (see Jahan and Ahmed (1997)).

The Barind area has a complex geological setup with heterogeneous lithology. It is dissected into several morphological blocks by numerous faults and lineaments. Hydrogeologically, the uplifted blocks are made up of older sediments with the intervening valleys of recent alluvium. The top sandy to silty-clay and fine sand forms the upper Aquitard of the area. The Pleistocene Modhupur Clay below constitutes the Composite Aquifer with a thickness of 10-60 m, which is the highest in the structurally elevated central horst block. Underlying the Composite Aquifer is the Main Aquifer composed of fine to coarse sand with gravel of Pleistocene Dupi Tila Formation (see Jahan and Ahmed (1997)).

### Climate

Although receives considerably less rainfall, the Barind area still experiences typical tropical monsoon climate and enjoys substantial amount of rainfall during June-October. With retreating monsoon in late October, groundwater recharge practically stops as rainfall – the principal source gradually wanes and ceases. November-February period is dry and cool with almost no precipitation. With increasing evapotranspiration, as soil loses moisture groundwater level gradually starts falling. March heralds in by pushing the mercury upward along with the groundwater abstraction. Consequently, the lowering of water level accelerates and the groundwater level hits its bottom limit – the maximum depth to water level. The Barind Tract endures high temperature in March-May period. June arrives with the monsoon rainfall and the water level begins to recharge again; the process continues throughout the entire post monsoon period. The aquifer fills itself

to the fullest just as the monsoon phases out. The groundwater level reaches its top limit closest to the land surface – the minimum depth to water level.

Records of Bangladesh Meteorological Department (BMD) show that the temperature of the Barind varies from 5° to 45° C with a mean of 25.5° C. Humidity is minimum (40%-70%) in winter and at the beginning of pre-monsoon. During the rest of the year, it is higher – varying from 70% to 100%. As per Bangladesh Water Development Board (BWDB) data, the annual evaporation of the area ranges from 370 mm to 1120 mm.

### 3. DATA AND METHODS

The database for the present study constitutes the depth to water level of observation wells at 50 Permanent Hydrographic Stations (PHS) in the Barind area. These wells, two in each of the 25 *upazillas* under BMDA command area, routinely collect the depth to water level measured below ground surface. Monthly water level data of observation wells from all 50 PHS for the period 1986-2004 was analyzed in this study. The data was processed to obtain the maximum and minimum depths to water level. To determine the trends, water level was regressed over the time span. A simple linear regression analysis was performed with water level as the dependent variable and time the independent one using the Ordinary Least Square (OLS) method, which simply computes the “best” fit line through the data. Jahan *et al.* (2004) and Hassan (2005) did exactly similar study with the same data set but they employed the raw data for their regression analyses that generally yielded very low R-sq and insignificant impact of the trend over time in almost all of the cases and those results are not shown for brevity.

For this type of time series data there is evidence (Ryan (1997)) that the OLS method often can produce poor fits. A number of nonparametric and smoothing techniques are available in the literature (see Ryan (1997), Chatterjee and Hadi (2006), Montgomery *et al.* (2008)) to produce better fit when the OLS fails to do so and since this is a time series data we believe that the moving average regression will be a much better choice. We employ a five-year moving average instead of raw data in formulating the regression equation in order to obtain more significant results in terms of coefficient of determination (R-sq) and the corresponding probability (p-value).

The slope or inclination of the regression equation would indicate the trend of depth to water level: a positive value would mean an increasing trend while a negative would suggest a decreasing trend. The larger the magnitude of the slope, the higher the increase or decrease is. A zero magnitude slope stands for no change.

Trend maps of water level of the Barind for both maximum and minimum depths were constructed. Combining these two, a composite trend map of the area was also prepared in order to delineate distinct zones with regard to their groundwater potentiality.

#### 4. RESULTS AND DISCUSSION

The regression analyses of data from all 50 PHS show that the slope of the maximum and minimum equations vary from -0.14 to 0.71 and -0.16 to 0.4 respectively. That means, on a yearly basis, the maximum depth to water level varies from 0.14m decrease to 0.71m increase while the minimum level from 0.16m decrease to 0.4m increase. The slopes of regression line together with p-value and R-sq of both maximum and minimum depth to water level equations are listed in Table-1. The results are generally significant in terms of coefficient of determination and p-value of the slope of the moving average regression. As we have already mentioned that Jahan *et al.* (2004) and Hassan (2005) reported that almost every least squares regression is insignificant for this data but the moving average regression as given in Table 1 show some stunning results. For the maximum depth of water level 36 out of 50 PHS's (72% of the stations) show significant trend at the 5% level and at the 10% level this number is 38. For the minimum depth of water level 27 out of 50 PHS's show significant trend at the 5% level while this number is 29 at the 10% level. These results clearly show the advantage of using the moving average regression over the least squares for this type of data.

**TABLE 1:** Five-year moving average trends of depth to groundwater level

PHS No.	Location	Maximum Depth to Water Level			Minimum Depth to Water Level		
		Slope	p-value	R-sq	Slope	p-value	R-sq
1	Baliadanga, Nawabganj	0.34417	<b>0.000</b>	0.918	-0.08726	0.173	0.149
2	Khamar, Nawabganj	0.29242	<b>0.000</b>	0.770	-0.05183	0.354	0.072
3	Gomastapur, Gomastapur	-0.08972	<b>0.046</b>	0.343	0.27359	<b>0.000</b>	0.892

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**TABLE 1**(continued): Five-year moving average trends of depth to groundwater level

PHS No.	Location	Maximum Depth to Water Level			Minimum Depth to Water Level		
		Slope	p-value	R-sq	Slope	p-value	R-sq
4	Boalia, Gomastapur	-0.20428	<b>0.002</b>	0.631	-0.24096	<b>0.000</b>	0.929
5	Shibganj, Shibganj	-0.02412	0.248	0.119	-0.06780	<b>0.031</b>	0.357
6	Nayanaobhanga, Shibgonj	-0.04393	<b>0.002</b>	0.580	-0.05390	<b>0.048</b>	0.288
7	Gohalbari, Bholahat	0.41871	<b>0.000</b>	0.873	-0.03778	0.517	0.360
8	Bholahat, Bholahat	0.33242	<b>0.000</b>	0.917	-0.06149	0.120	0.190
9	Nachole, Nachole	0.71142	<b>0.000</b>	0.971	0.032646	<b>0.001</b>	0.590
10	Nizampur, Nachole	0.63321	<b>0.000</b>	0.939	-0.04639	<b>0.001</b>	0.637
11	Talondo, Tanore	0.18076	<b>0.000</b>	0.766	0.21414	<b>0.000</b>	0.888
12	Kamargaon, Tanore	0.16987	<b>0.000</b>	0.862	0.10607	<b>0.009</b>	0.447
13	Godagari, Godagari	0.40389	<b>0.000</b>	0.834	0.34287	<b>0.000</b>	0.910
14	Matikata, Godagari	0.19255	<b>0.000</b>	0.967	0.37569	<b>0.000</b>	0.859
15	Haripur, Paba	0.17780	0.127	0.479	0.39653	<b>0.002</b>	0.931
16	Naohata, Paba	0.22105	<b>0.031</b>	0.728	0.05348	0.452	0.148
17	Pannanagar, Durgapur	0.09449	0.217	0.447	0.06807	0.128	0.592
18	Daluabari, Durgapur	0.08077	<b>0.026</b>	0.851	0.06350	0.283	0.362
19	Auchpara, Bagmara	0.24028	0.062	0.738	0.1213	<b>0.000</b>	0.996
20	Hamirkustsha, Bagmara	0.16183	<b>0.050</b>	0.658	0.14884	<b>0.003</b>	0.964
21	Bajubagha, Bagha	-0.13970	0.112	0.624	0.19406	<b>0.024</b>	0.858
22	Arani, Bagha	-0.07468	0.347	0.292	0.08890	0.143	0.565
23	Mohanpur, Mohanpur	0.3632	0.189	0.489	0.13106	0.055	0.757
24	Raighati, Mohanpur	0.1991	0.388	0.253	-0.0406	0.779	0.030
25	Salua, Charghat	0.12845	<b>0.008</b>	0.862	-0.01742	0.813	0.016
26	Charghat, Charghat	0.07591	0.064	0.618	-0.05588	0.441	0.154
27	Silmaria, Puthia	0.1049	0.359	0.211	-0.01568	0.684	0.046
28	Puthia, Puthia	0.26499	<b>0.012</b>	0.825	-0.06140	0.289	0.271
29	Jagadishpur, Badalgachi	0.09245	<b>0.005</b>	0.570	-0.07991	<b>0.001</b>	0.705
30	Kola, Badalgachi	0.15226	<b>0.017</b>	0.485	-0.02235	0.489	0.055
31	Patnitala, Pantitala	0.06688	<b>0.008</b>	0.454	0.23002	<b>0.000</b>	0.812
32	Nazipur, Patnitala	0.05177	<b>0.000</b>	0.734	0.11074	<b>0.000</b>	0.836
33	Enayetpur, Mahadevpur	0.07230	<b>0.000</b>	0.686	0.09119	<b>0.000</b>	0.811
34	Bhimpur, Mahadevpur	0.09865	<b>0.001</b>	0.612	0.029966	<b>0.002</b>	0.561
35	Srimantapur, Niamatpur	0.16158	<b>0.000</b>	0.979	0.27540	<b>0.000</b>	0.852
36	Parail, Niamatpur	0.70985	<b>0.000</b>	0.908	-0.02576	0.087	0.224
37	Manda, Manda	0.19484	<b>0.000</b>	0.754	0.01748	0.436	0.051
38	Prasadpur, Manda	0.15764	<b>0.000</b>	0.716	-0.01039	0.631	0.020
39	Surly, Aihai, Shapahar	0.66611	<b>0.000</b>	0.815	0.11686	<b>0.000</b>	0.793

**TABLE 1**(continued): Five-year moving average trends of depth to groundwater level

PHS No.	Location	Maximum Depth to Water Level			Minimum Depth to Water Level		
		Slope	p-value	R-sq	Slope	p-value	R-sq
40	Rasulpur, Aihai, Sapahar	0.54303	<b>0.000</b>	0.898	0.13506	<b>0.000</b>	0.915
41	Gangguria, Porsha	0.58616	<b>0.000</b>	0.980	0.40408	<b>0.000</b>	0.757
42	Nithpur, Porsha	0.07389	<b>0.009</b>	0.446	-0.01584	0.191	0.138
43	Aranagar, Dhamoirhat	0.04976	<b>0.001</b>	0.606	0.04189	0.124	0.186
44	Omar, Dhamoirhat	0.18091	<b>0.000</b>	0.797	0.27404	<b>0.000</b>	0.868
45	Raninagar, Raninagar	0.12598	<b>0.043</b>	0.680	-0.11945	0.221	0.344
46	Kaligram, Raninagar	0.05762	0.093	0.547	0.1180	<b>0.004</b>	0.897
47	Panchupur, Atrai	0.05646	0.221	0.344	-0.1614	<b>0.000</b>	0.983
48	Bhopara, Atrai	0.17487	<b>0.010</b>	0.842	-0.09885	<b>0.002</b>	0.925
49	Naogaon Paurasabha	-0.04688	0.430	0.162	-0.02845	0.505	0.118
50	Tilakpur, Naogaon	-0.05283	0.491	0.125	0.06473	0.156	0.433

By plotting the slope values and contouring, maximum and minimum trend maps of depth to water level for the study area were also constructed (Figures 2 and 3). The maximum trend map shows that most of the Barind area is bounded by +ve slope values implying that the maximum depth to water level is increasing. That means, in the Barind water level is falling as a rule during the lean season; the highest rate of fall as high as 0.71m/year is recorded in Niamatpur *upazilla*. Out of a total 25 *upazillas*, an exception to this is found only in part of Naogaon in the east; most of Bagha in the southeast; and parts of Shibganj, Gomastapur, Nachole and Bholahat in the west, where the water level is found to be rising with the highest rate (0.14m/year) in Bagha.



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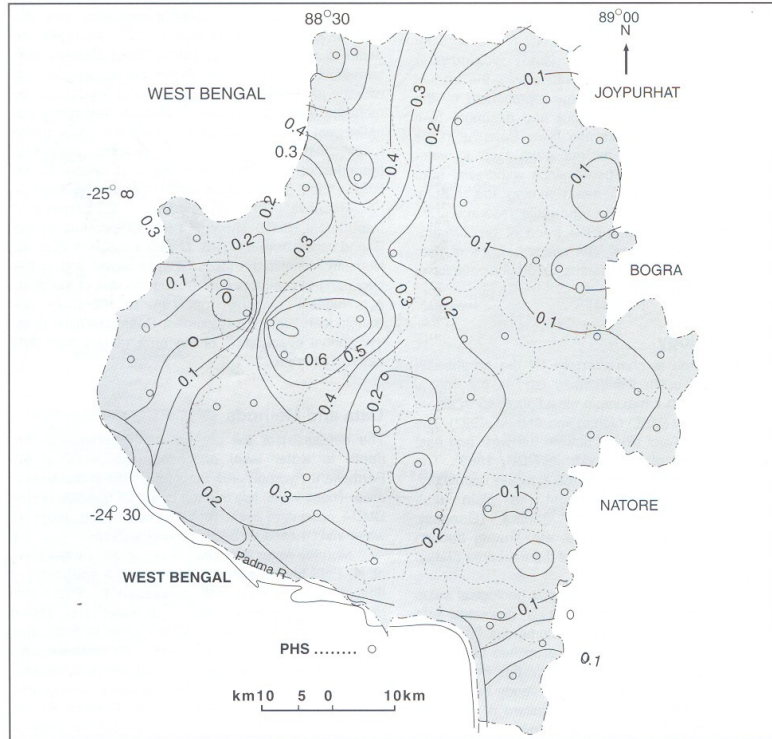


Figure 2: Contour map of regression line slope for maximum depth to water level (Database: 1996-2004)

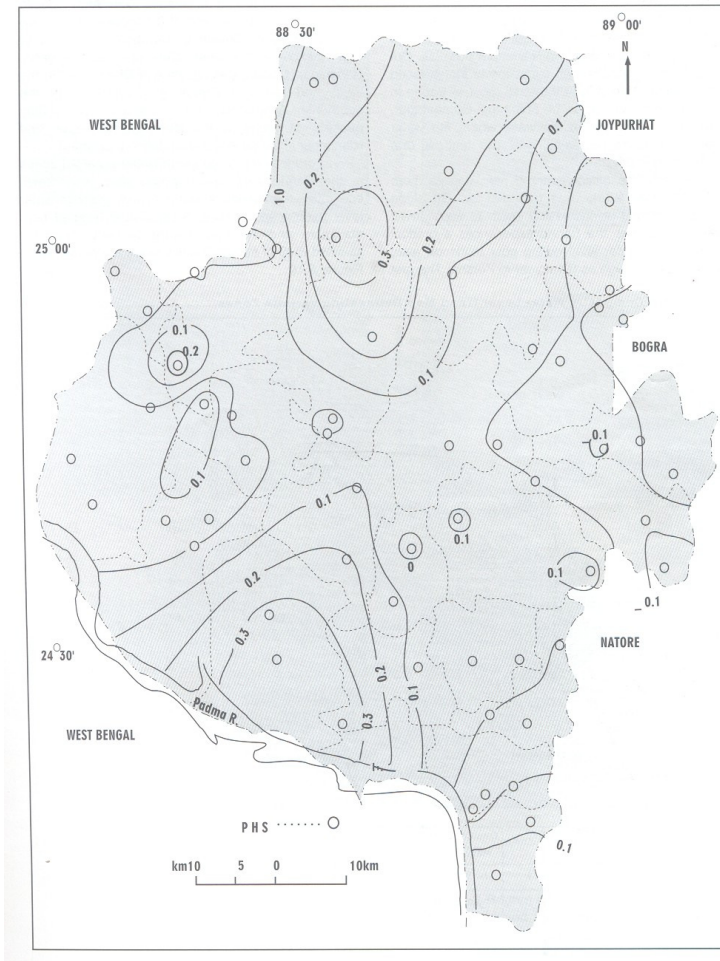


Figure 3: Contour map of regression line slope for minimum depth to water level (Database: 1996-2004)

Similarly, the minimum trend map depicts more than 2/3 of the study area bounded by +ve slope values connoting an increasing depth to water level. Hence, in general, the Barind experiences a gradual decline in the water level during the post monsoon too; the decline is as high as 0.4m/year in Porsha. The rest – less than 1/3 of the region, where we see an ascending trend in the water level, is principally located in the west, east and southeast with Atrai *upazilla* showing the highest ascent of 0.16m/year. They are parts of Shibganj, Bholahat, Nawabganj, Gomastapur and Nachole

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in the west; parts of Atrai, Naogaon, Raninagar, Manda, Badalgachi and Dhamoirhat in the east; and parts of Puthia and Charghat in the southeast. Additionally, there are a couple of tiny pockets of rising water level in Mohanpur and Niamatpur in the central Barind during this period.

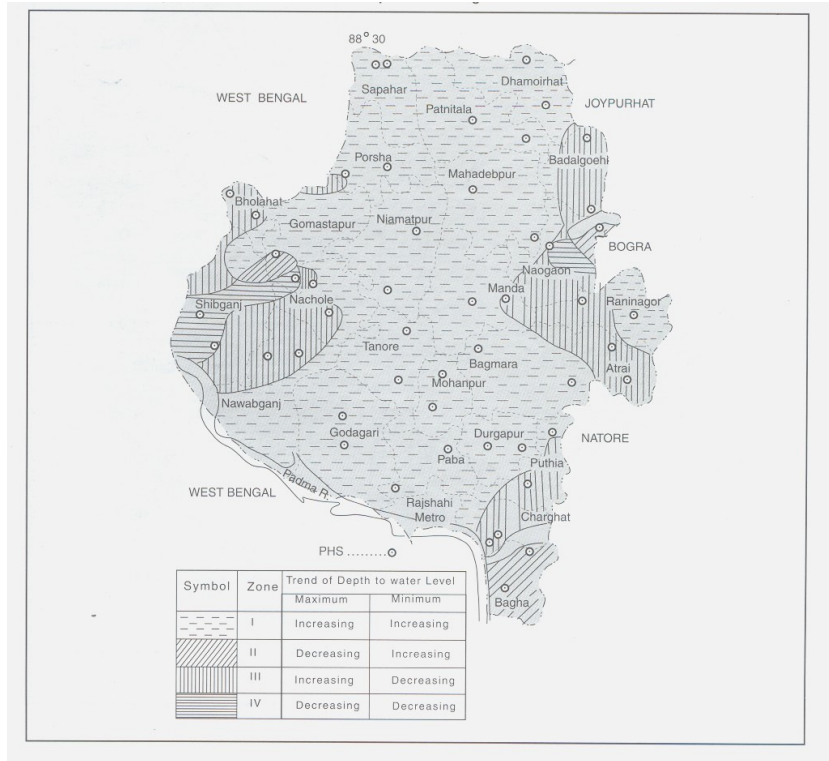


Figure 4: Composite water level trend map delineating various zones

In order to delineate groundwater potential zones in the Barind area, a composite map was drawn integrating the maximum and minimum depth to water level trend maps (see Figure 4). Trend lines of both maximum and minimum depths to water level for selected PHS of all four distinct zones are presented in Figure 5.

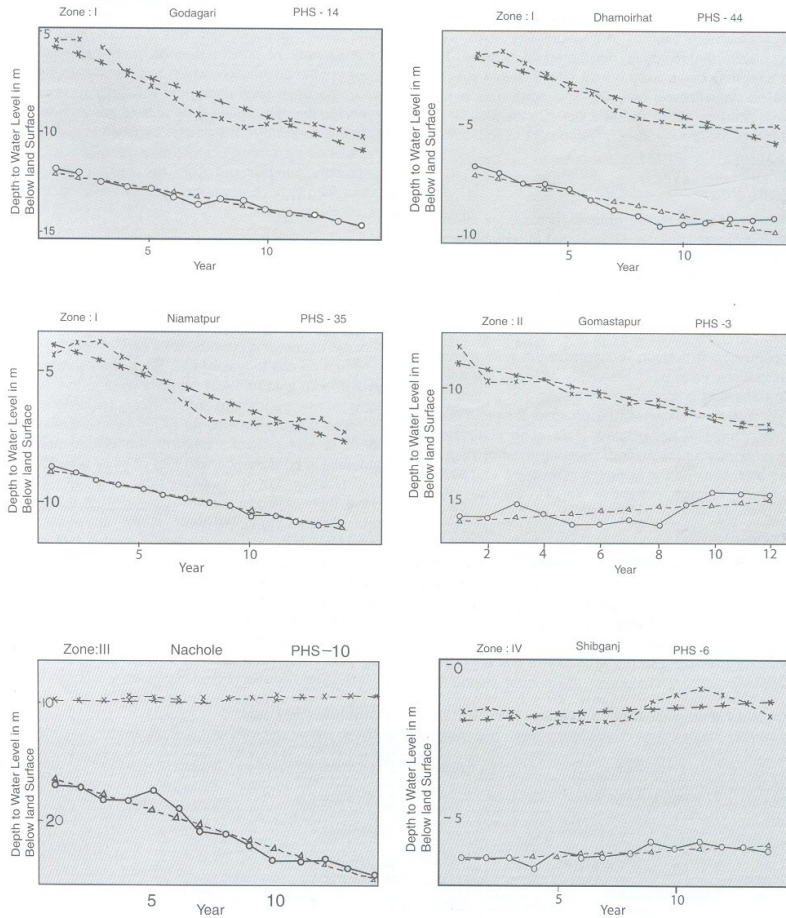


Figure 5: Five-year moving average of depths (maximum and minimum) to water level versus time for selected PHS's representing various zones (Database: 1996-2004)

### Zone-I

This zone covers about 2/3 of the BMDA command area. Not included in this zone are only parts of Nawabganj, Shibganj, Bholahat, Gomastapur and Nachole in the west; parts of Atrai, Naogaon, Raninagar, Manda, Badalgachi and Dhamoirhat in the east; most of Bagha, parts of Charghat and Puthia in the southeast; and a couple of tiny enclaves in Mohanpur and Niamatpur in the central Barind. It is characterized by continual increase in

both maximum and minimum depths to water level. In the dry season the water level is gradually deepening to meet the growing withdrawal demand. At the same time, the rate of replenishment through recharge during the wet season is also lagging behind. This may give rise to a subsurface situation where sagging of inter-granular voids within the aquifer that remained dewatered takes place. This, in turn, may decrease the total effective void space of the aquifer affecting its yield. This zone may already have started losing its potential. Consequently, the prospect for groundwater development of this zone is negative.

### **Zone-II**

This small zone shows gradual increase in minimum depth to water level even though the maximum depth is actually decreasing a little. During the lean period, possibly as a result of lessening of withdrawal volume, one sees corresponding rise in the water level. However, the wet season recharge is failing to reach its mark; and the water level is gradually falling. Lack of replenishment through recharge in the post monsoon time may have been adversely affecting the aquifer. The situation is similar, even though not as grave, to that of Zone-I. Likewise, the prospect for groundwater development is not positive. This zone comprises a small portion of the Barind covering most of Bagha in the southeast; part of Naogaon in the east; and parts of Shibganj, Gomastapur and Bholahat in the west.

### **Zone-III**

This zone, which is less than 1/4 of the Barind, includes parts of Nawabganj, Shibganj, Bholahat, Gomastapur and Nachole in the west; parts of Atrai, Naogaon, Raninagar, Manda, Badalgachi and Dhamoirhat in the east; and parts of Puthia and Charghat in the southeast. It has also got a couple of tiny enclaves in Mohanpur and Niamatpur in the central Barind. The zone is characterized by gradual increase in maximum depth to water level but slight decrease in minimum depth. The gradual decline of the water level in the dry period is indicative of inflating withdrawal demand of this zone. Here, the replenishment of aquifer through recharge is still in excess of the abstraction, which has resulted in a slight rise in the water level during wet season. Although, presently the recharge is quite able to make up for the drafted groundwater, the aquifer situation is essentially unstable as increasing amount of groundwater is being continually pumped out from the storage that may before long go out of control permanently damaging the aquifer potential.

#### **Zone-IV**

This zone covers only a small portion of the Barind area: just part of Naogaon in the east and parts of Shibganj, Gomastapur and Nachole in the west. It depicts decreasing trends for both maximum and minimum depth to water level. Here, the rise of water level in both lean and wet seasons point to the zone's potential to support more groundwater abstraction.

The present findings as to the overall increasing depth to water level trends of the Barind area is generally in consonance with that of other researchers (e.g. Hassan (2005)). However, Jahan *et al.* (2004) found quite different results using almost the same data. Interestingly, in their study they have had somewhat dissimilar methodology. Instead of using maximum depth to water level, they opted for an "average of March through May" from monthly database. Similarly, they used an "average of October and November" in lieu of minimum depth to water level. Moreover, they employed the raw data for their regression analyses that would generally yield very low R-sq and corresponding insignificant regression coefficients. Our study clearly shows the advantage of employing moving average regression for the data. We observe from Table 1 that the majority of the permanent hydrographic stations show significant regression individually and Figure 5 shows regressions are significant for all four zones constructed by contour map.

### **5. CONCLUSION**

Moving average regression analyses of the monthly depths to water level data reveal increasing trends for both maximum and minimum in Zone I which is about 2/3 of the Barind area. Future groundwater development of this part of the Barind, showing a gradual fall of the water level in both dry and wet seasons, is not advisable. In addition, most of the remaining area, located in the west, east and southeast, that we call Zone II and Zone III experience decline in the water level either in the post monsoon period or during the lean season rendering further development prospects for groundwater nil or slim. Only a small portion of the BMDA command area, Zone IV, located in Shibganj and Gomastapur in the west and Naogaon in the east, still enjoys potential for further groundwater development.

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